



## Motivation

- EUV photomasks reflect light with both attenuation and phase delay
- The phase impacts imaging, especially with regard to aberrations (defocus)
- Both the real and imaginary parts of the complex electric field must be known accurately before SMO

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## Objectives

- Measure the real and imaginary parts of the mask reflection function to the highest possible accuracy
- Explore the potential and limitations of scatterometry vs traditional imaging vs coded-aperture imaging

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## The Problem

- Optical phase cannot be directly observed, but can be recovered computationally
- We explore several hardware and software solutions for line-space gratings that can be implemented at CXRO

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## Traditional phase-retrieval

- Solve for phase from multiple intensity images using nonlinear least-squares
  - Susceptible to error in initial guess

$$\min_E \sum_i \left\| \sqrt{I_i} - E * H_i \right\|_2^2$$

- $I_i$  – measured intensity image
- $E$  – mask's complex field
- $H_i$  – Imaging system PSF
- Multiple images w/different  $H_i$  needed

## Algorithmic improvement: PhaseLift

- Computationally intensive, but not susceptible to error in initial guess
- Images are *linear* in *rank-1 matrix*  $EE^*$ :

$$I_i = \text{diag}[F^* \text{diag}[\tilde{H}_i] \tilde{E} \tilde{E}^* \text{diag}[\tilde{H}_i^*] F] \\ = \mathcal{L}_i\{\tilde{E} \tilde{E}^*\} = \mathcal{L}_i\{X\}$$

$$\min_X \alpha \text{Trace}[X] + \sum_i \left\| I_i - \mathcal{L}_i\{X\} \right\|_2^2$$

Small trace promotes low-rank solutions

Data consistency term (least-squares)

Ref: Candès, E. J., Strohmer, T., & Vershynski, V. (2013). Phaselift: Exact and stable signal recovery from magnitude measurements via convex programming. *Communications on Pure and Applied Mathematics*, 66(8), 1241-1274.

## Hardware improvement: coded aperture

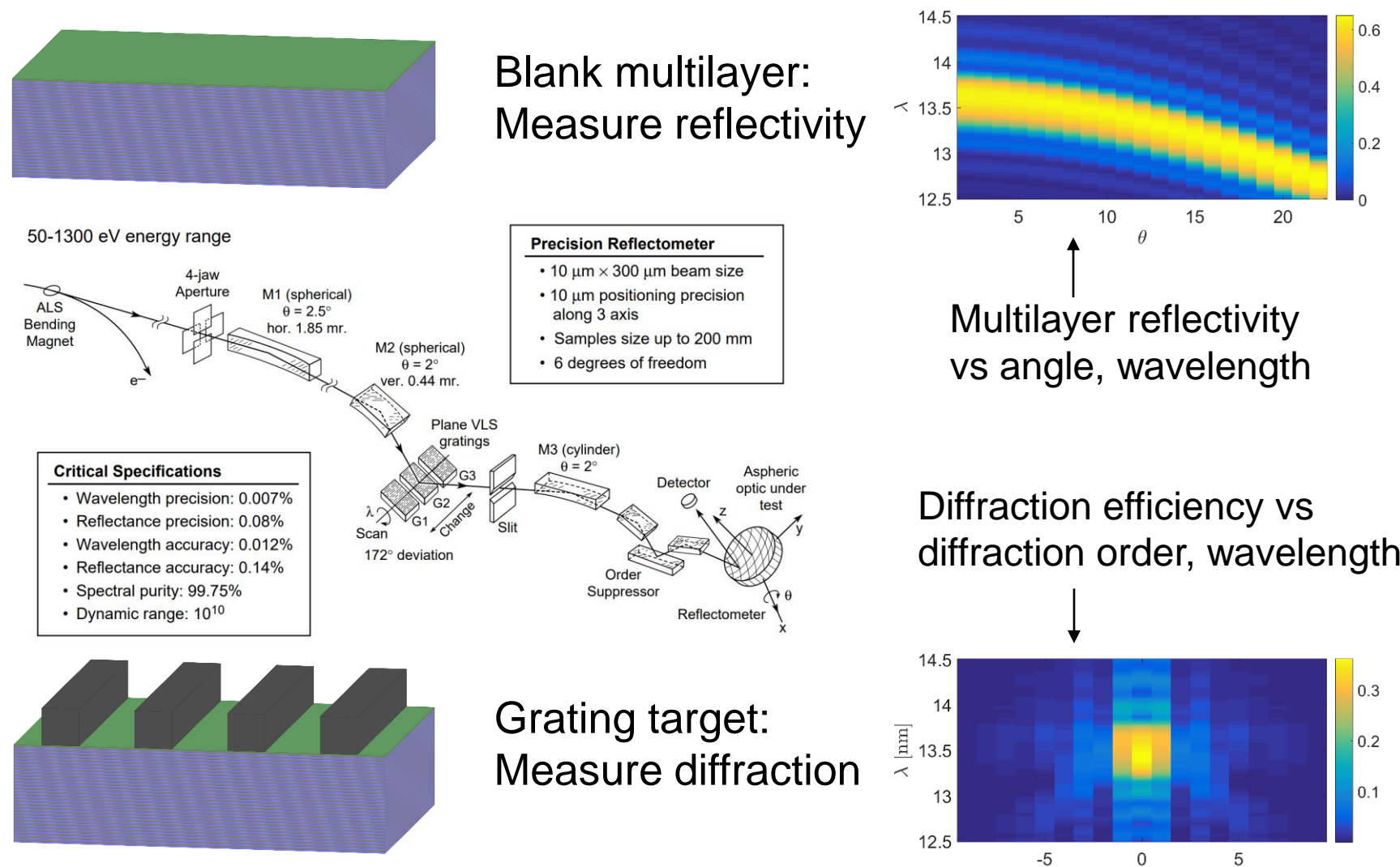
- Self-referencing interferometry:
  - If you can phase-shift *only* the DC (carrier), phase can be solved directly:

$$I_{\phi_i}[x_j] = (1, \cos \phi_i, \sin \phi_i) \begin{pmatrix} a_{1,j} \\ a_{2,j} \\ a_{3,j} \end{pmatrix} \\ a_{2,j} \propto \text{Re}(E[x_j]), a_{3,j} \propto \text{Im}(E[x_j])$$

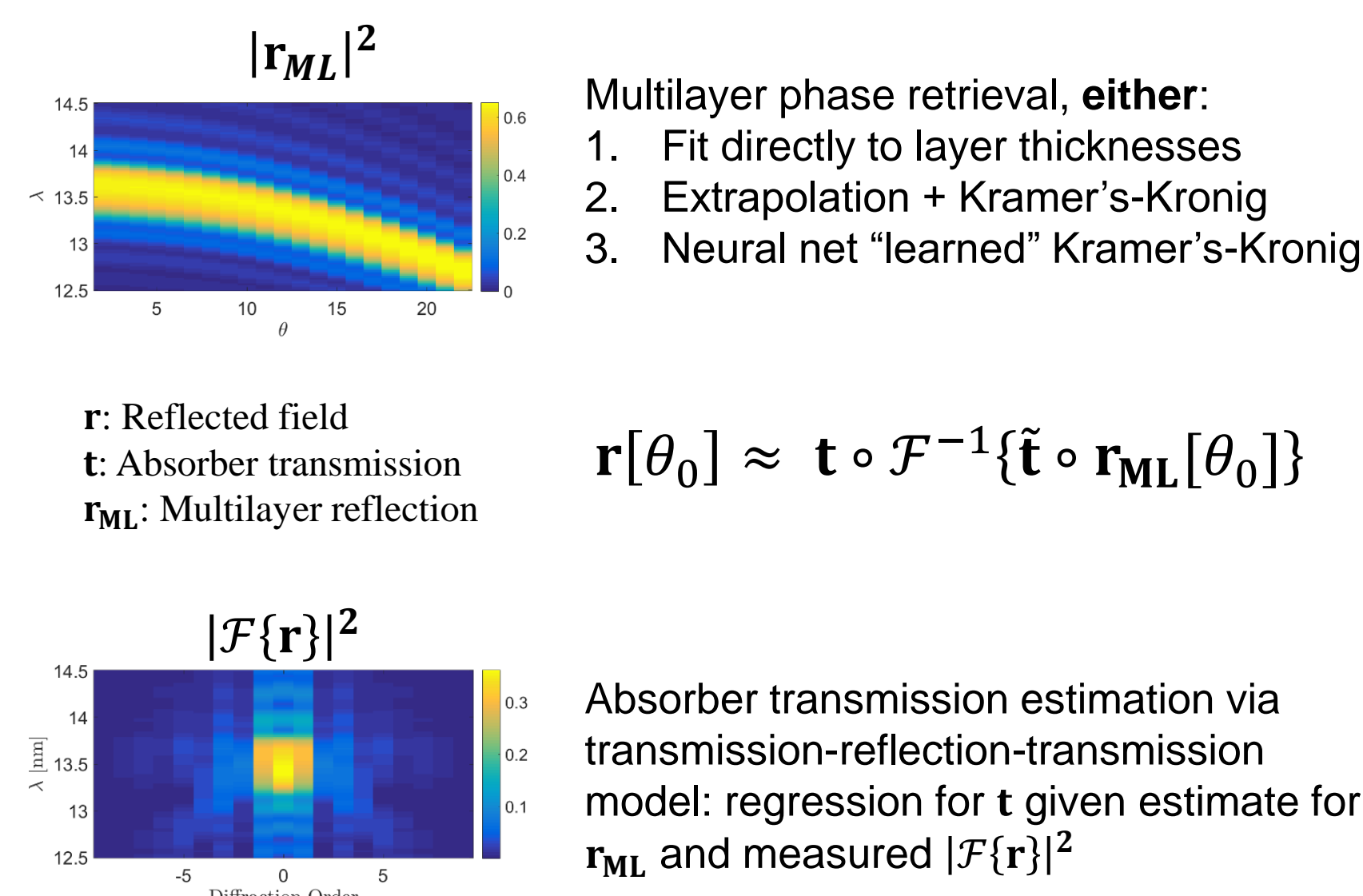
- Implementation with coded-apertures
- Insight into coded-aperture design

Ref: Bon, P., Maucort, G., Wattellier, B., & Monneret, S. (2009). Quadriwave lateral shearing interferometry for quantitative phase microscopy of living cells. *Optics express*, 17(15), 13080-13094.

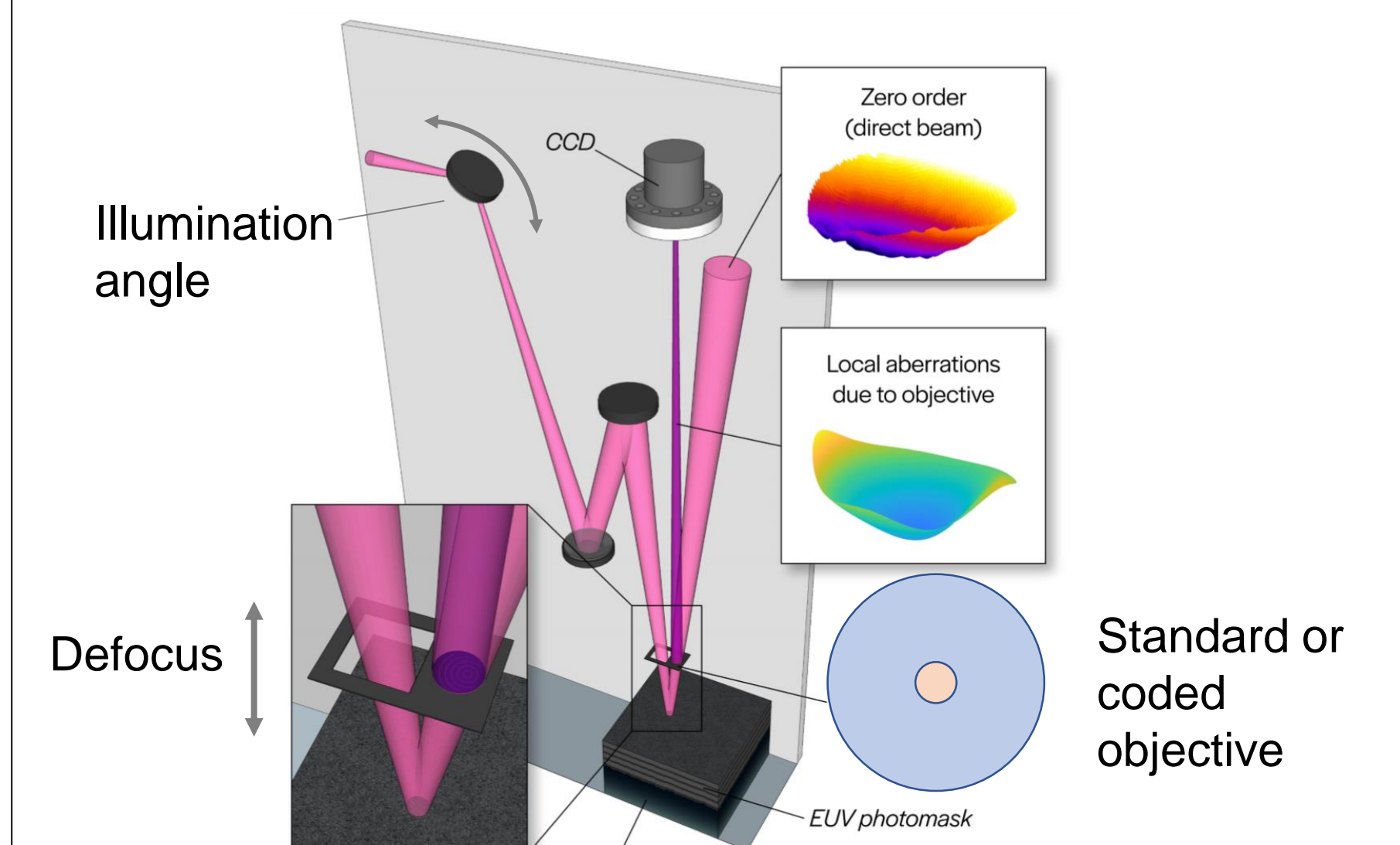
## Non-imaging approach: scatterometry



## Scatterometry analysis



## SHARP EUV imaging system

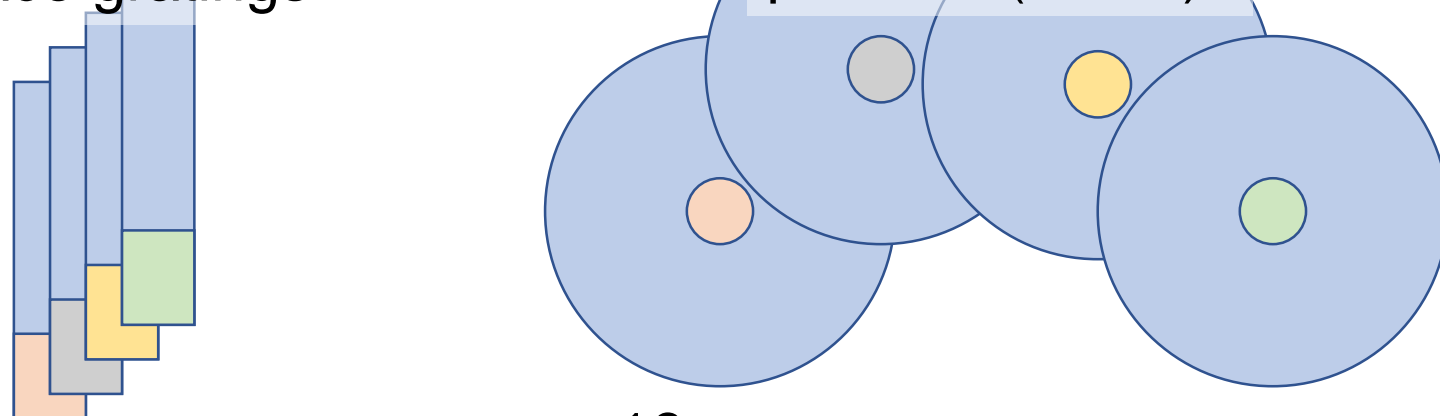


## Coded aperture: phase-shifting DC

- SHARP: custom zone-plate (ZP) objectives
- Set of coded ZPs for phase retrieval
- 0 order passes through phase-shifted region, scattered light imaged normally

1D ZPs: line-space gratings

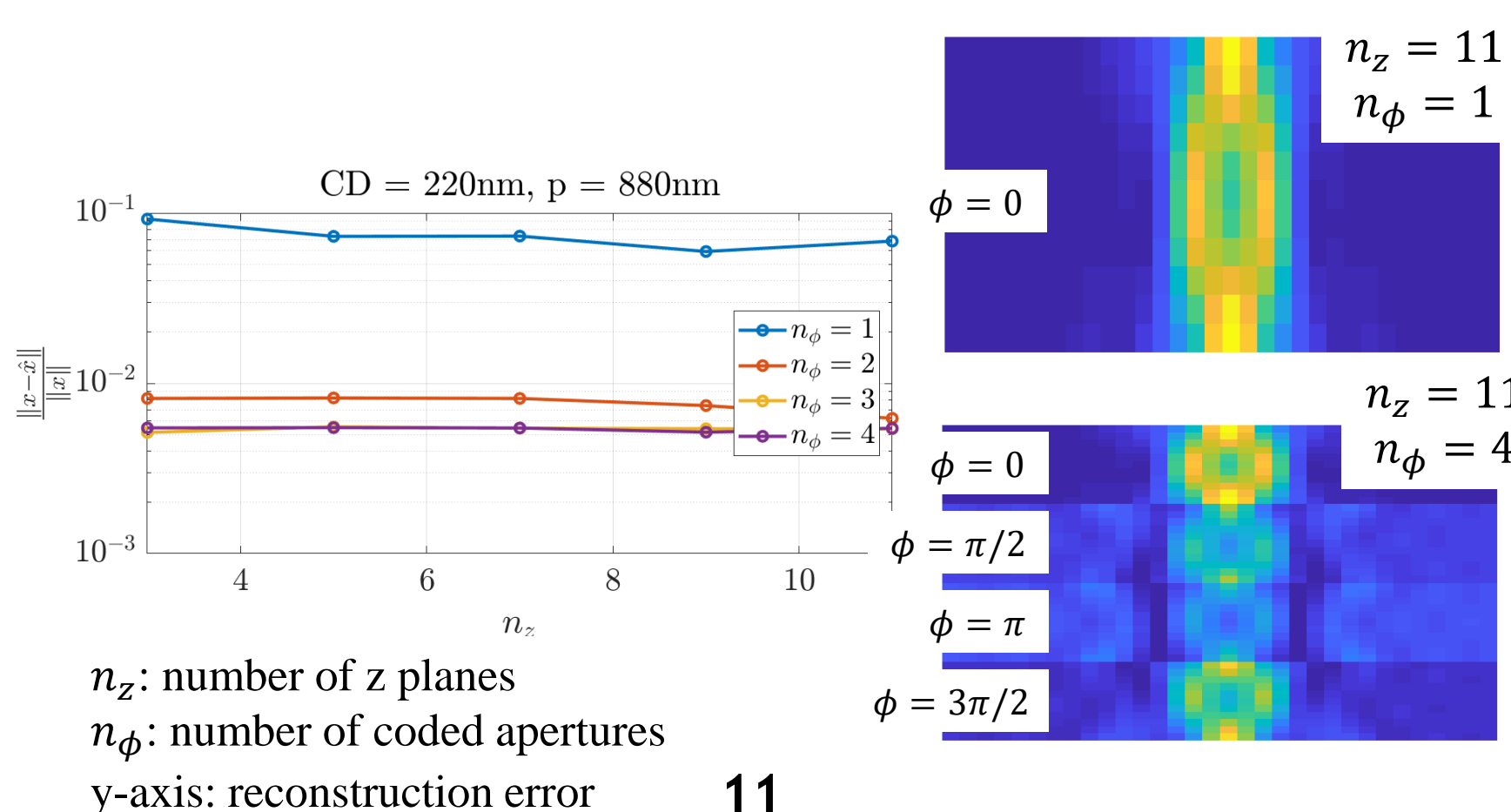
2D ZPs: arbitrary patterns (future)



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## Initial studies using PhaseLift

- Key result: coded aperture improves accuracy over defocus for larger pitch



## Future Goals

- Fabricate set of DC phase-shifted zone-plates
  - 1D, 2 orientations for H/V features
- Conduct experiments at ALS using measurement modalities discussed

### Acknowledgment

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